

Special case of LMTD

$$(1) \quad \theta_1 = \theta_2 = \theta$$

$$\theta_m = \frac{\theta_2 - \theta_1}{\ln \theta_2 / \theta_1}$$

$$\theta_m = \frac{0}{\ln 1} = \frac{0}{0}$$

Indeterminate form.

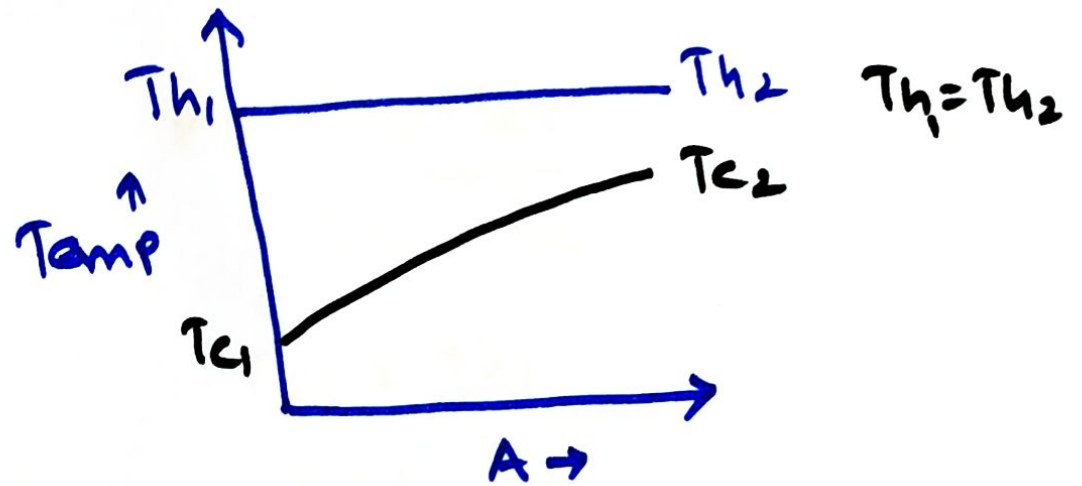
L'Hospital's Rule

$$\lim_{\theta_2 \rightarrow \theta_1} \frac{\frac{\partial}{\partial \theta_1} (\theta_2 - \theta_1)}{\frac{\partial}{\partial \theta_1} (\ln \theta_2 / \theta_1)}$$

$$= \frac{1}{1/\theta_1} = \theta_1 = \theta_2 = \theta$$

$$Q = UA\theta_1 = UA\theta_2 = UA\theta$$

LMTD for Condenser.



$$\theta_1 = Th_1 - Tc_1$$

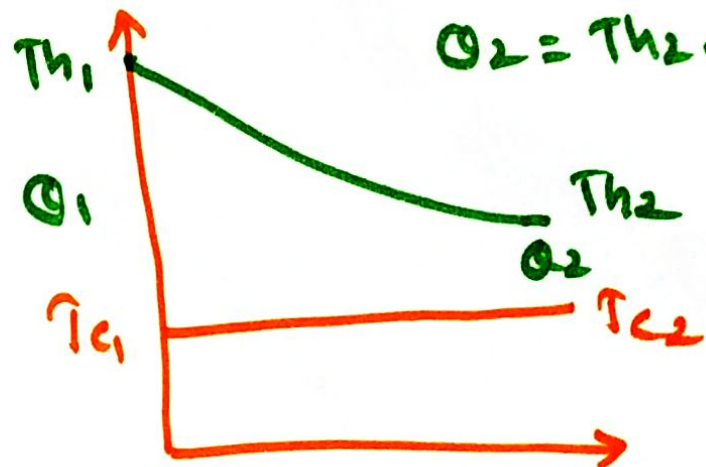
$$\theta_2 = Th_2 - Tc_2$$

$$\theta_m = \frac{\theta_1 - \theta_2}{\ln \theta_1 / \theta_2}$$

Evaporator.

$$\theta_1 = Th_1 - Tc_1$$

$$\theta_2 = Th_2 - Tc_2$$



⇒ Correction factors for multipass Heat Exchangers

$$Q = UA \Delta T_m F$$



$$R = \frac{(m \cdot c)_{\min}}{(m \cdot c)_{\max}}$$

$$m_c c_c (\hat{T}_2 - \hat{T}_1) = m_h c_h (T_{h1} - T_{h2})$$

$$R = \frac{T_{h2} - T_{h1}}{\hat{T}_2 - \hat{T}_1}$$

$$R = \frac{\text{Temp. Drop of hot fluid}}{\text{Temp. rise of cold fluid}}$$

$$P = \frac{T_{c2} - T_{c1}}{T_{h1} - T_{c1}}$$

$$T_{c2} = T_{h1}$$

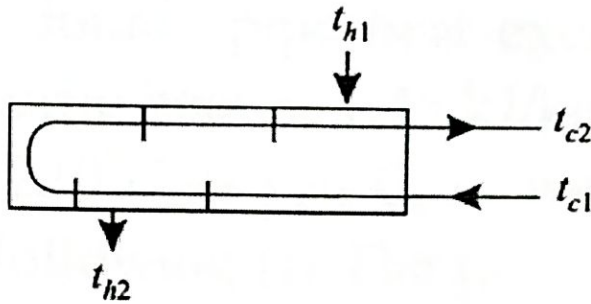
$$P = 1$$

$$\hat{T}_2 = \hat{T}_1$$

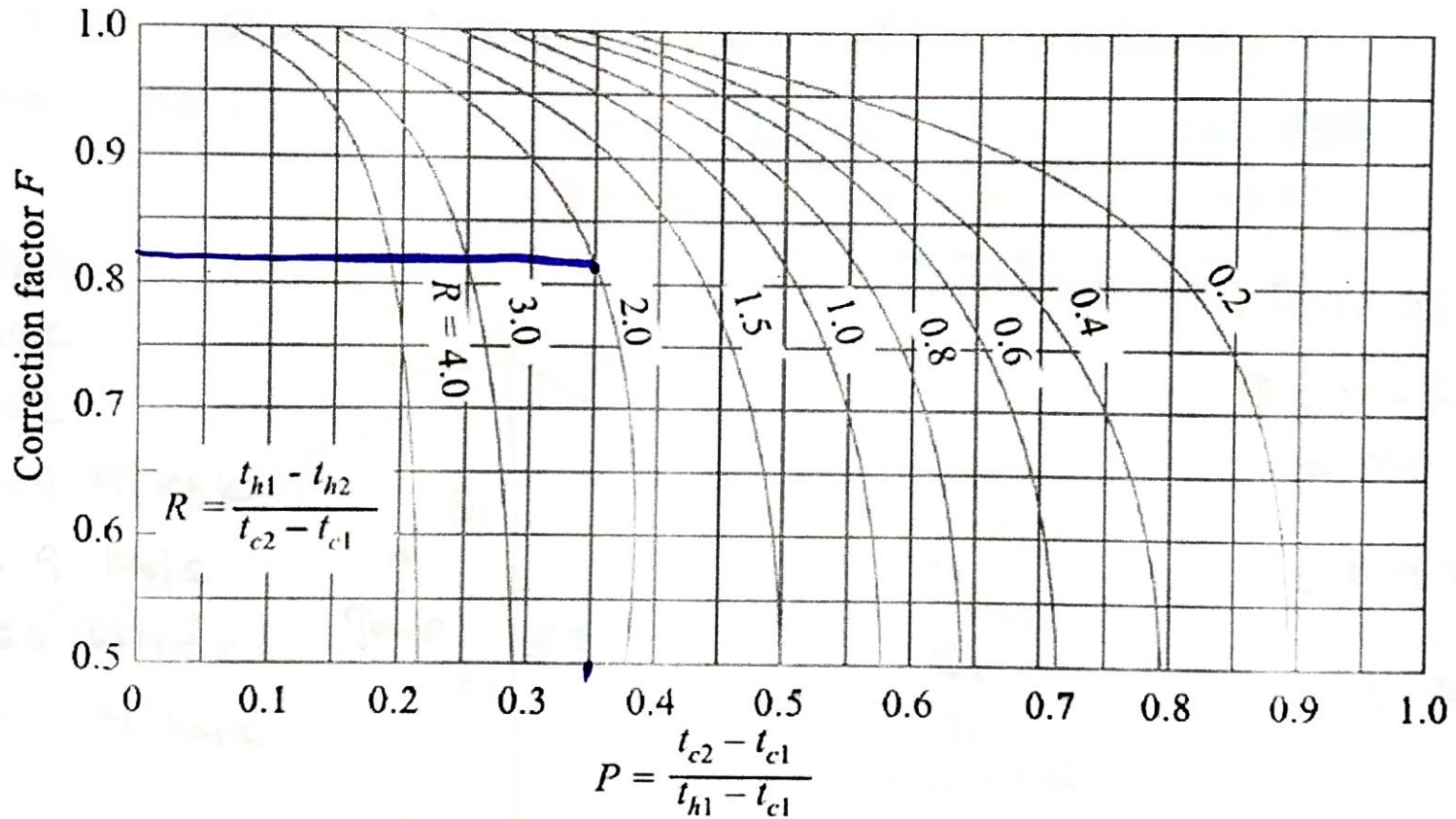
$$P = 0$$

P varies in the range of 0 to 1

$$F = 0.825$$



$$R = 2.0$$
$$P = 0.35$$



Correction factor plot for heat exchanger with one shell pass and two, four or any multiple of tube passes.