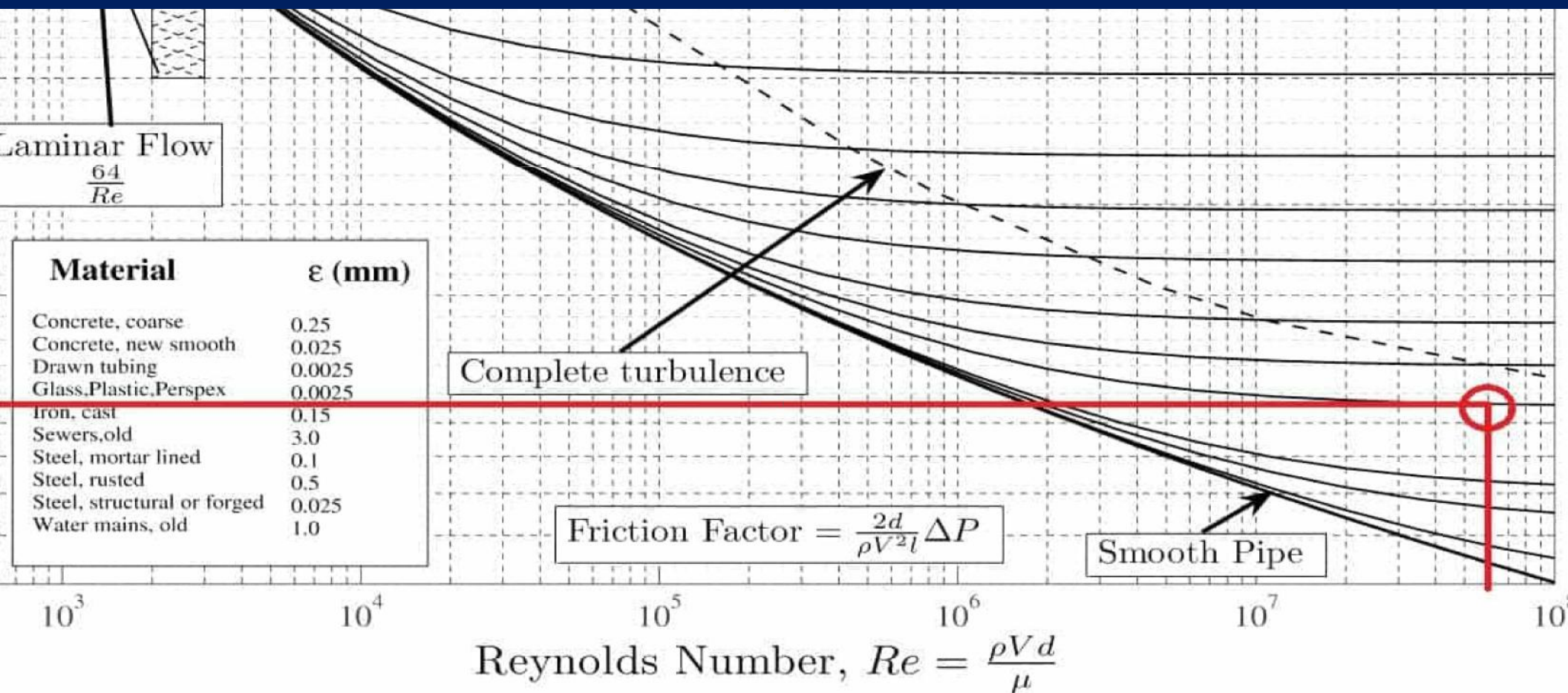


# Moody Diagram

# Turbulent Flow (MOODY DIAGRAM)

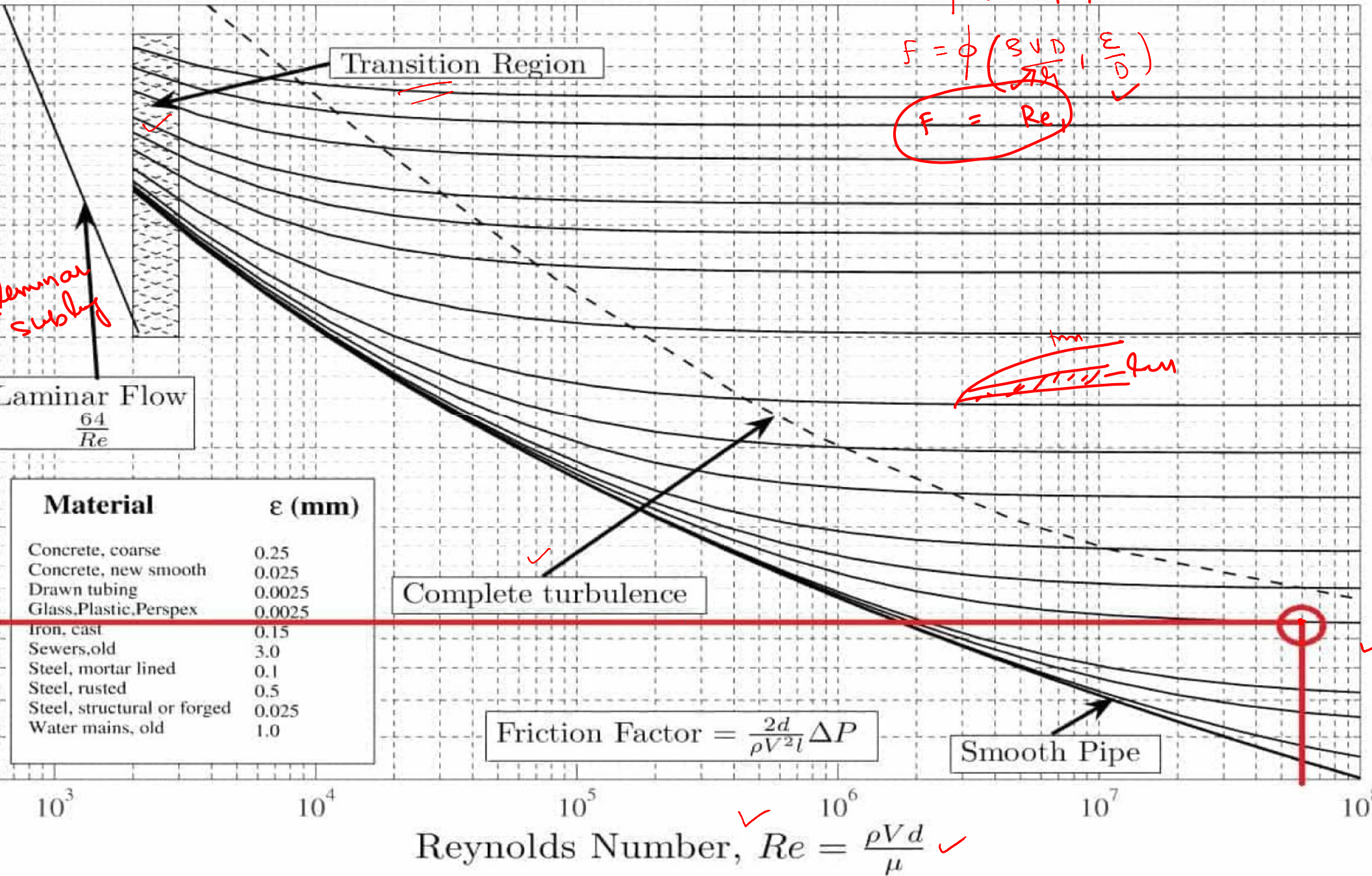


# Moody Diagram

$$f = \phi(V, D, \rho, \mu, \epsilon)$$

$$f = \phi\left(\frac{\rho V D}{\mu}, \frac{\epsilon}{D}\right)$$

$f = Re^{-1}$



# MOODY DIAGRAM

is Very useful in Practical World

$$f \rightarrow \epsilon/d, Re$$

because we can find the value of Friction co-efficient for the given Reynolds's Number and for the relative roughness of the smooth or rough pipes ✓



# MOODY DIAGRAM

was made by Moody and Nikuradse

They have performed lots of practical and then draw a graph for the three related criteria.

Means this is made by three axis.

Left Vertical axis represents friction coefficient (  $f$  )

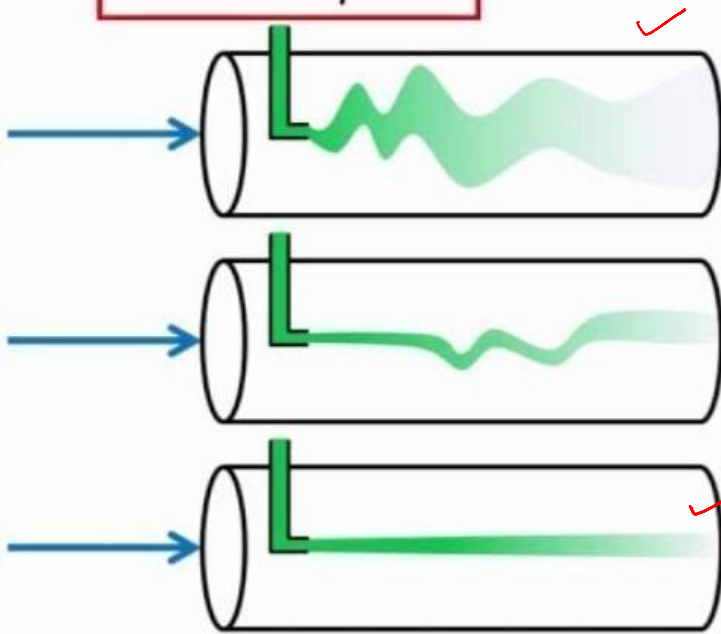
Horizontal axis represents Reynolds's Number (  $Re$  )

Right Vertical axis represents Relative roughness (  $\epsilon/D$  )

Means It gives the value of  $f$  against the  $Re$  for the value of  $\epsilon/D$  .

# Turbulent Flow, Transition Flow & Laminar Flow

$$\text{Re} = \frac{\rho V_{\text{avg}} D}{\mu}$$



$\text{Re} > 4000$

**turbulent** (unpredictable, rapid mixing)

$2000 < \text{Re} < 4000$

**transitional** (turbulent outbursts)

$\text{Re} < 2000$

**laminar** (predictable, slow mixing)

From Darcy-Weisback Formula and for turbulent flow

$$h_f = \frac{C_f l V^2}{2gD}$$

$$h_f = \frac{K_f l V^2}{2gD}$$

Roughness of pipe =  $\epsilon$  ✓

Diameter of pipe =  $D$  ✓

Relative Roughness of pipe ✓ =  $\epsilon/D$

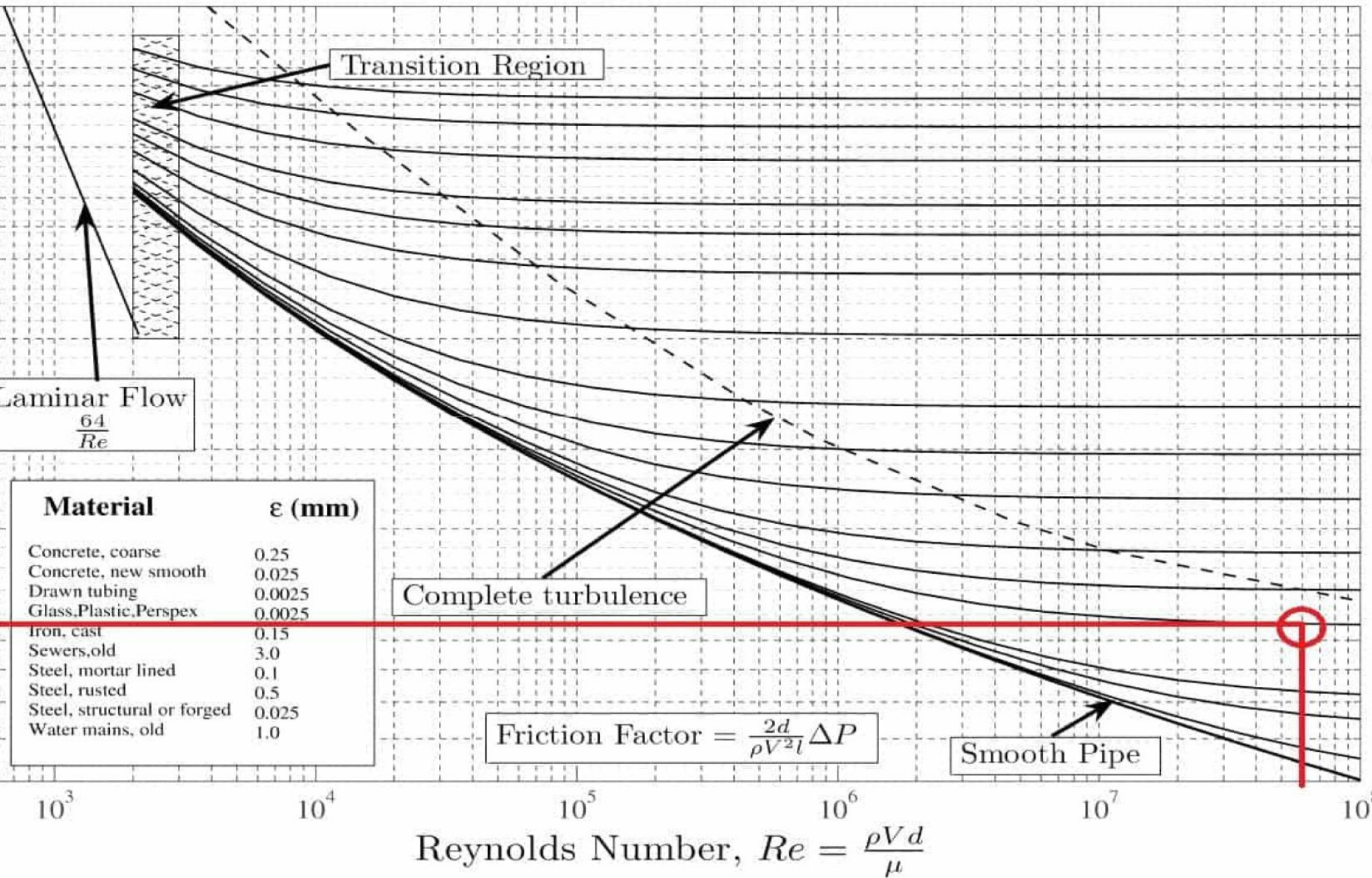
Laminar Flow:  $f = \frac{64}{\text{Re}}$

Smooth Pipe Turbulent Flow:  $f = \frac{0.316}{\text{Re}^{1/4}}$

Completely Turbulent Flow:  $f = \left[ 1.14 + 2 \log_{10} \left( \frac{D}{\varepsilon} \right) \right]^{-2}$

Transition Region:  $f = \left\{ -2 \log_{10} \left[ \frac{(\varepsilon/D)}{3.7} + \frac{2.51}{\text{Re} (f^{1/2})} \right] \right\}^{-2}$

# Moody Diagram





# Application of MOODY DIAGRAM

to find out value of Friction co-efficient –  $f$

to find out the value of head loss  $h_f$

to find out the value of Discharge –  $Q$

to find out the diameter of pipe -  $D$

A pipe of 30 cm in diameter and 500m long is carrying oil having sp. gravity 0.9 and viscosity 0.08 poise. The oil flow rate is 120 litre per second. Calculate the head loss in the pipe and power required to maintain the flow.

$$f = 0.079(\text{Re})^{1/4}$$

$$h_f = \frac{4fL v^2}{2gD}$$

Given Data

$$30 \times 10^{-2} \text{ m}$$

$$500 \text{ m}$$

$$= 0.9$$

$$900 \text{ kg/m}^3$$

$$0.08 = 0.008 \text{ N}\cdot\text{s/m}^2$$

$$120 \text{ lps}$$

$$120 \times 10^{-3} \text{ m}^3/\text{sec}$$

$$0.079(\text{Re})^{1/4}$$

$$Q = Av$$

$$\text{Velocity of oil} = \frac{Q}{A} = \frac{120 \times 10^{-3}}{\frac{\pi}{4} \times (30 \times 10^{-2})^2} = 1.6976 \text{ m/sec}$$

$$\text{Re} = \frac{\rho v D}{\mu} = \frac{900 \times 1.6976 \times 30 \times 10^{-2}}{0.008} = 57,295.78$$

$$f = 0.079 \times (\text{Re})^{1/4} = 0.079 \times (57,295.78)^{1/4} = 0.0051$$

$$h_f = \frac{4fL v^2}{2gD} = \frac{4 \times 0.0051 \times 500 \times (1.69)^2}{2 \times 9.81 \times 30 \times 10^{-2}} = 5 \text{ m of oil}$$

$$P = \frac{\rho g Q h}{1000} \text{ kW} = \frac{900 \times 120 \times 10^{-3} \times 9.81 \times 5}{1000} = 5.2974 \text{ kW}$$

Water Tank 4 km away from college hostel. Water supplies 150 litres per student. The strength of student in hostel is 1000. The total water required is pumped into the tank in night time for 6 hours. Calculate the diameter of pipe if head loss is limited to 25 m. Assume  $f=0.0018$

Given

$$L = 4 \times 10^3 \text{ m}$$

$$h_f = 25 \text{ m}$$

$$f = 0.0018$$

$$N = 1000 \text{ student}$$

$$Q = 150 \text{ lit/student}$$

$$t = 6 \text{ hr}$$

$$Q = 150 \text{ lit/student}$$

$$= 150 \times 1000 \text{ lit}$$

$$= \frac{150 \times 1000}{6} \text{ lit/hr}$$

$$= \frac{150 \times 10^3 \times 10^{-3} \text{ m}^3/\text{s}}{6 \times 3600}$$

$$Q = 0.006944 \text{ m}^3/\text{sec}$$

$$V = \frac{Q}{A} = \frac{0.006944}{\frac{\pi}{4} D^2} = \frac{0.008842}{D^2} \text{ m/sec}$$

$$h_f = 25 \text{ m}$$

$$h_f = \frac{4fLv^2}{2gD}$$

$$25 = \frac{4 \times 0.0018 \times 4 \times 10^3 \times \left(\frac{0.008842}{D^2}\right)^2}{2 \times 9.81 \times D}$$

$$25 = 1.1476 \times 10^{-4} \times \frac{1}{D^5}$$

$$D^5 = 4.59 \times 10^{-6}$$

$$D = 0.085579 \text{ m}$$

$$\boxed{D = 8.56 \text{ cm}}$$