

Q.1 In a counter flow heat double pipe heat exchanger, water is heated from 25°C to 65°C by oil with specific heat of 1.45 kJ/kg K and mass flow rate of 0.9 kg/s . The oil is cooled from 230°C to 160°C . If overall Heat transfer coefficient is $420 \text{ W/m}^2 \text{ }^{\circ}\text{C}$. Calculate following (i) The rate of heat transfer (ii) The mass flow rate of water, and (iii) The surface area of heat exchanger (GTU-Dec-2013)

Given Data

$$T_{c1} = 25^{\circ}\text{C}$$

$$T_{c2} = 65^{\circ}\text{C}$$

$$T_{h1} = 230^{\circ}\text{C}$$

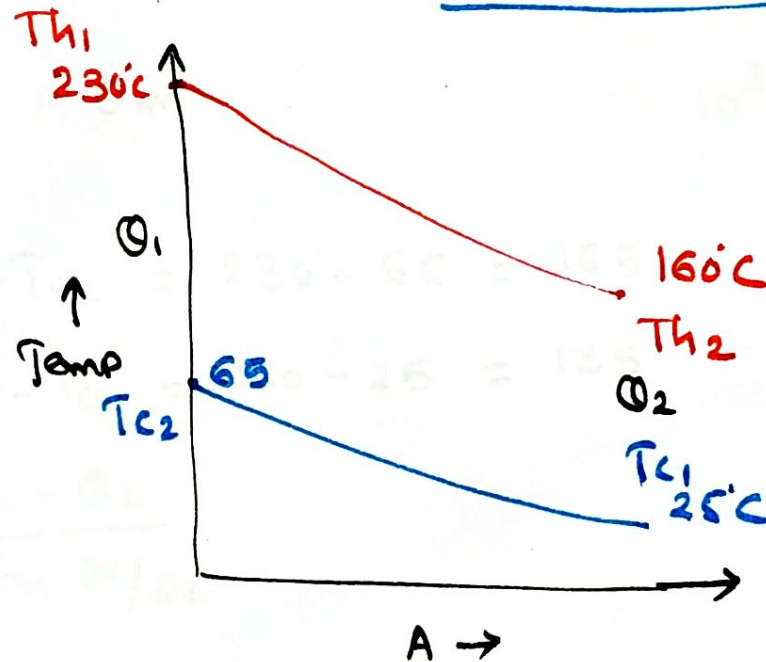
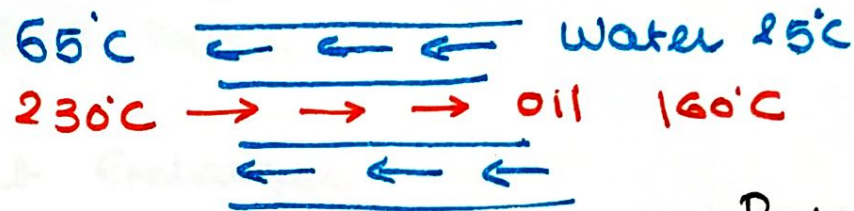
$$T_{h2} = 160^{\circ}\text{C}$$

$$C_{ph} = 1.45 \text{ kJ/kgK}$$

$$m_h = 0.9 \text{ kg/s}$$

$$U = 420 \text{ W/m}^2\text{K}$$

$$C_{pc} = 4.2 \text{ kJ/kgK}$$



(1) Rate of Heat Transfer

$$\begin{aligned} \phi &= m_h C_h (T_{h1} - T_{h2}) \\ &= m_c C_c (T_{c2} - T_{c1}) \\ &= 0.9 \times 1.45 \times (230 - 160) \\ &= 91.35 \text{ kJ/sec} \end{aligned}$$

(2) mass flow rate of water

$$\dot{Q}_m = \dot{Q}_c$$

$$m_h c_h (T_{h1} - T_{h2}) = m_c c_c (T_{c2} - T_{c1})$$

$$0.9 \times 1.45 \times (230 - 160) = m_c \times 4.2 \times (65 - 25)$$

$$m_c = 0.545 \text{ kg/sec}$$

(3) Surface area of Heat Exchanger

$$\dot{Q} = UA \Delta T_m$$

$$10^3 \times 91.35 = 420 \times A \times 149.5$$

$$\Delta T_1 = T_{h1} - T_{c2} = 230 - 65 = 165$$

$$\Delta T_2 = T_{h2} - T_{c1} = 160 - 25 = 135$$

$$A = 1.45 \text{ m}^2$$

$$\Delta T_m = \frac{\Delta T_1 - \Delta T_2}{\ln \Delta T_1 / \Delta T_2}$$

$$= \frac{165 - 135}{\ln(165/135)} = 149.5^\circ\text{C}$$

Q.2 Hot air at 66 °C is cooled up to 38 °C by means of cold air at 15.5 °C. mass flow rates of hot and cold air are 1.25 kg/s and 1.6 kg/s respectively. Specific heat of hot and cold air are 1.05 kJ/kg k, $U = 80 \text{ W/m}^2\text{K}$, find the area of the heat exchanger for parallel flow configuration. If the same heat exchanger is operated in counter flow mode, find the area required.

(GTU-May 2014)

Given Data

$$T_{h1} = 66^\circ\text{C}$$

$$T_{h2} = 38^\circ\text{C}$$

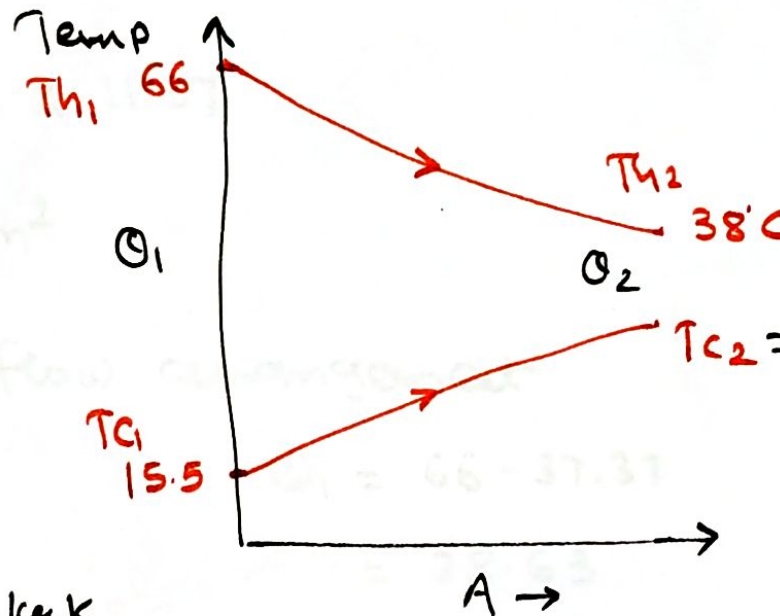
$$T_{c1} = 15.5^\circ\text{C}$$

$$m_h = 1.25 \text{ kg/s}$$

$$m_c = 1.6 \text{ kg/s}$$

$$c_{ph} = c_{pc} = c = 1.05 \text{ kJ/kgK}$$

$$U = 80 \text{ W/m}^2\text{K}$$



$$\theta_1 = T_{h1} - T_{c1}$$

$$= 66 - 15.5$$

$$= 50.5$$

$$\theta_2 = T_{h2} - T_{c2}$$

$$= 38 - 37.37$$

$$= 0.63$$

$$\theta_m = \frac{\theta_1 - \theta_2}{\ln \theta_1 / \theta_2}$$

$$= \frac{50.5 - 0.63}{\ln(50.5/0.63)}$$

$$\theta_m = 11.37^\circ\text{C}$$

$$\Phi = \Phi_h = \Phi_c$$

$$m_h c_{ph} (T_{h1} - T_{h2}) = m_c c_{pc} (T_{c2} - T_{c1})$$

$$1.25 (66 - 38) = 1.6 (T_{c2} - 15.5)$$

$$T_{c2} = 37.37^\circ\text{C}$$

$$\Phi = U A \Delta T_m$$

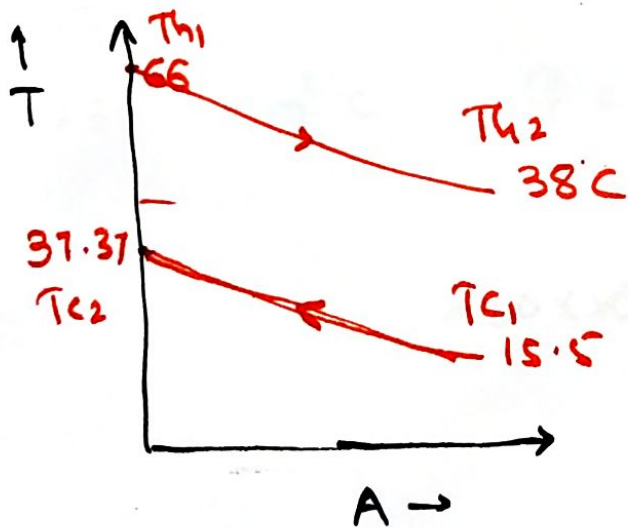
$$\begin{aligned}\Phi &= m_h c_h (T_{h1} - T_{h2}) \\ &= 1.25 \times 1.05 \times (66 - 38) \\ &= 36.75 \text{ kJ/sec}\end{aligned}$$

$$10^3 \times 36.75 = 80 \times A \times 11.37$$

$$A = 39.26 \text{ m}^2$$

Case - II

Counter flow arrangement



$$\Delta T_1 = 66 - 37.37$$

$$= 28.63$$

$$\Delta T_2 = 38 - 15$$

$$= 23$$

$$\Delta T_m = \frac{\Delta T_1 - \Delta T_2}{\ln \Delta T_1 / \Delta T_2} = \frac{28.63 - 23}{\ln \frac{28.63}{23}} = 25.71^\circ \text{C}$$

$$\Phi = U A \Delta T_m$$

$$36.75 \times 10^3 = 80 \times A \times 25.71$$

$$A = 17.87 \text{ m}^2$$

Q.3 A steam condenser is transferring 250 KW of thermal energy at a condensing temperature of 65⁰C. the cooling water enter the condenser at 20⁰C with a flow rate of 7500 kg/hr. calculate the log mean temperature difference. If overall heat transfer co efficient for condenser surface is 1250 w/m²-deg, what surface area is required to handle this load. (GTU- Dec 2014)

Given Data

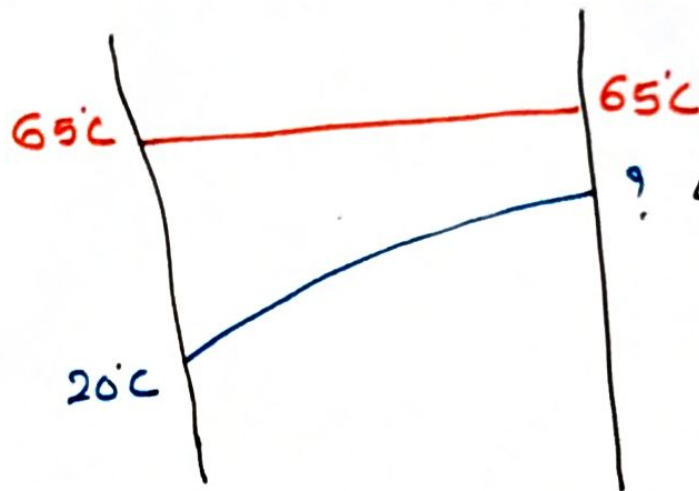
$$T_{h1} = T_{h2} = 65^{\circ}\text{C}$$

$$T_{c1} = 20^{\circ}\text{C}$$

$$\Phi = 250 \times 10^3 \text{ W}$$

$$m_c = \frac{7500}{3600} \text{ kg/sec}$$

$$U = 1250 \text{ W/m}^2 \cdot \text{C}$$



$$\theta_1 = 65 - 20 = 45$$

$$\theta_2 = 65 - 48.51 = 16.49$$

$$\theta_m = \frac{\theta_1 - \theta_2}{\ln \theta_1 / \theta_2} = \frac{45 - 16.49}{\ln 45 / 16.49}$$

$$\theta_m = 28.3$$

$$\Phi = m_f h_{fg} = m_c c_c (T_{c2} - T_{c1})$$

$$250 \times 10^3 = \frac{7500}{3600} \times 4.2 \times (T_{c2} - 20)$$

$$T_{c2} = 48.51$$

$$\Phi = U A \theta_m$$

$$250 \times 10^3 = 1250 \times A \times 28.3$$

$$A = 8.979 \text{ m}^2$$